

# Industrial Organisation

Lecture 1: Introduction to IO

Tom Holden

<http://io.tholden.org/>

# Key info: Contact details

- ▶ Email: [t.holden@surrey.ac.uk](mailto:t.holden@surrey.ac.uk)
- ▶ Standard office hours:
  - Thursday, 12–1PM + 3–4PM, 29AD00
- ▶ However, during term:
  - **CLASSES** will be run in the first hour.
  - Thursday, 12–1, in room 40AD00
  - If anyone turns up.
- ▶ For private problems:
  - Come to my office between 3–4PM.
  - Ideally, e–mail first so I know to wait for you.
  - Other times are possible by e–mail appointment.

# Key info: Web presence

- ▶ Course website is: <http://io.tholden.org/>
  - Going to SurreyLearn will just send you to this site.
- ▶ Has the last two years slides up already.
  - This year will have almost identical content to last year, so feel free to read ahead.
- ▶ Please use the comment facility on the site to ask about things you don't understand.
- ▶ This year, I will be videoing all lectures, and placing them on YouTube.

# Key info: Readings

- ▶ Main text:
  - Oz Shy: “Industrial organization: Theory and applications” 338.6 SHY
    - “Goldilocks” level difficulty (I hope).
- ▶ Alternative texts:
  - Jean Tirole, “The Theory of Industrial Organization” 338.6 TIR
    - A little difficult in places.
  - Jeffrey Church and Roger Ware, “Industrial Organisation: A strategic Approach”
    - Not quite right for our course, but it is available for free at:  
<http://is.gd/XHBLz4>
- ▶ Plus, as ever, Google & Wikipedia are your friends.

# Key info: Exams & timetable

- ▶ Midterm test (10%):
  - Very short answer section. One hour.
  - Week 6. Will provide mock.
- ▶ End of term test (20%):
  - Longer maths questions. Up to two hours.
  - Week 10. Again, there'll be a mock.
- ▶ Final exam (70%):
  - Very short answer section.
  - Rest is multi-part questions requiring both maths and discussion.
  - Again, there'll be a mock...

# Key info: Practice questions

- ▶ Oz Shy's book contains exercises.
  - Do them!
  - The answers are online at:  
<http://ozshy.50webs.com/bkman24.pdf>
- ▶ He has additional problems online at:  
<http://ozshy.50webs.com/io-exercises.pdf>
  - With solutions at <http://links.ozshy.com/io-solutions>
- ▶ I'll set a few other questions.

# Outline

- ▶ What is IO?
  - Aim of the course
- ▶ Some “revision”:
  - Demand curves
  - Consumer surplus
  - Cost functions
  - Profits
  - Welfare
  - Monopoly
- ▶ Note: There will be a lot of work on the board today.
  - It is important everyone get these basic bits of maths.
  - If you missed this lecture, ask a friend for notes, and study the readings.

# What is IO?

- ▶ IO *is not* the economics of manufacturing industries (as opposed to agriculture etc.).
- ▶ IO *is* the economics of:
  - the firm and its behaviour,
  - the structure of markets,
  - the regulation of markets.
- ▶ IO is the field of most economic consultants.



# Topics within IO

- ▶ Firm's decisions:
  - Entry, exit, mergers
  - R&D
  - Advertising
  - Capital investment
  - Pricing
- ▶ Market structure:
  - How do firms interact?
  - Why are some firms large?
  - Why are some industries highly concentrated?
- ▶ Competition policy:
  - Cartels and collusion
  - When should we regulate firms?

# Aim of the course

- ▶ IO is a big subject.
- ▶ Our aim will be cover enough theory that you could go on to think independently about practical questions.
- ▶ The theory is fun on its own though.
  - It's basically applied game theory.

# Demand curves (1 / 2) (OZ 3.2)

- ▶ Two ways of thinking about aggregate demand curves.
  - Homogeneous consumers, wanting multiple units.
  - Heterogeneous consumers, wanting one unit each.
  - Can you explain graphically how they emerge?
- ▶ We will usually denote demand curves by  $Q(p)$ .
  - And inverse demand curves by  $p(Q)$ .
  - Given  $Q(p)$  how do you derive  $p(Q)$ ?

# Demand curves (2 / 2)

- ▶ Two families of demand curves we will use a lot.
  - Linear:  $Q(p) = q_0 - q_1p$  or  $p(Q) = p_0 - p_1Q$ .
  - Iso-elastic (aka constant-elastic):  $Q(p) = cp^{-\alpha}$  or  $p(Q) = kQ^{-\beta}$ .
- ▶ How do we map from the parameters of the linear demand curve to the parameters of the linear inverse demand curve?
  - How do we go the other way?
  - How do we do the same for iso-elastic demand?

# Elasticity of demand

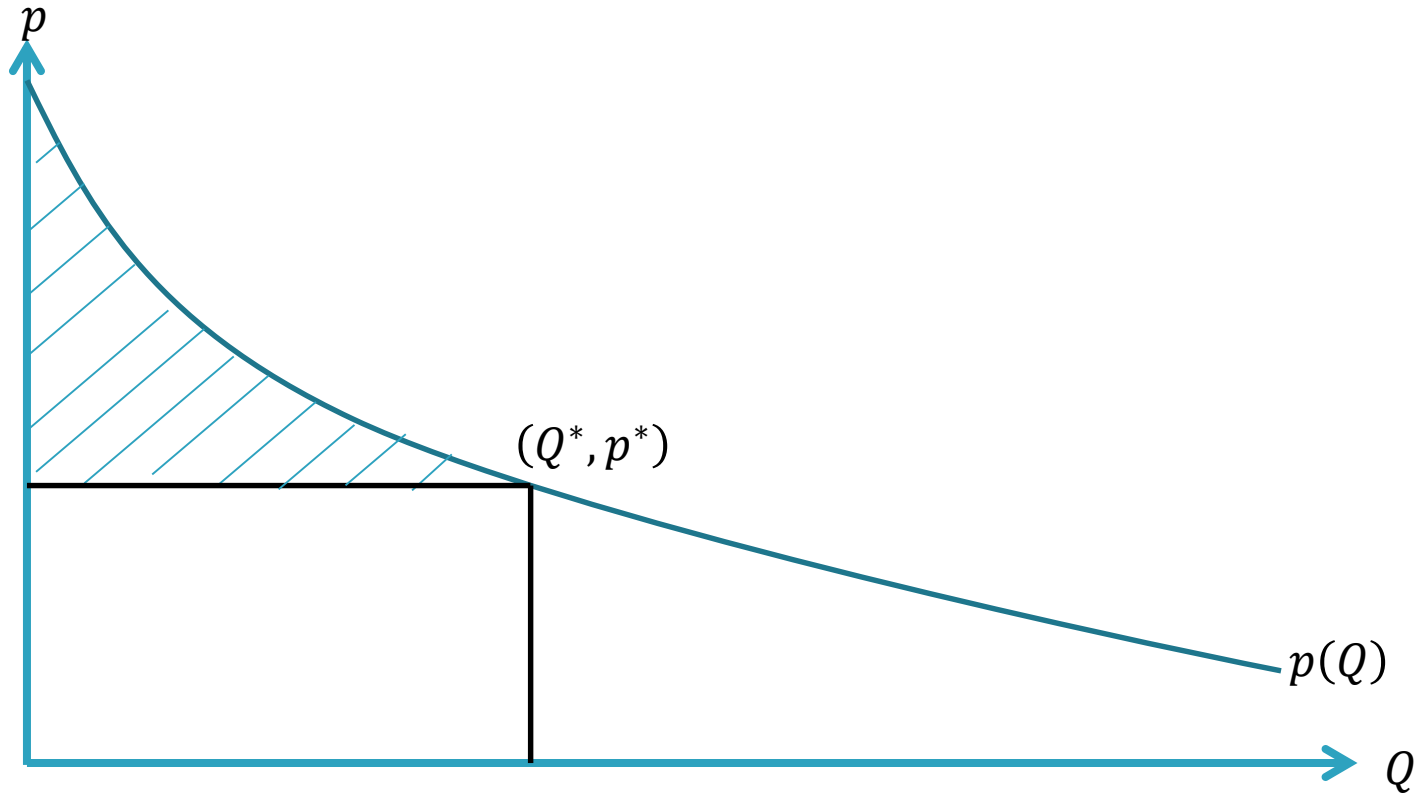
- ▶ The elasticity of demand at a quantity level  $Q$  is defined by:  $\eta_p(Q) := \frac{\partial Q(p)}{\partial p} \frac{p}{Q}$ .
- ▶ How do we find the elasticity of demand when we only have the inverse demand curve?
  - Hint: The Inverse Function Theorem states that:  $\frac{df^{-1}(x)}{dx} = \left[ \frac{df(x)}{dx} \right]^{-1}$ .
- ▶ Demand is elastic when  $|\eta_p(Q)| > 1$ .
- ▶ Demand is inelastic when  $|\eta_p(Q)| < 1$ .
- ▶ When is linear demand elastic?
- ▶ What is the elasticity of an iso-elastic demand curve?

# Consumer surplus (1 / 3)

## (OZ 3.3 has a special case)

- ▶ A consumer has utility  $U(Q) = v(Q) + M$ , where:
  - $Q$  is the quantity of some good,
  - $M$  is money left over for other goods.
  - What is this type of utility function called?
- ▶ Their income is  $Y$ , and the good costs  $p$ .
  - So their budget constraint says  $Y = pQ + M$ .
- ▶ Want to max:  $U(Q) = v(Q) + Y - pQ$ .
- ▶ FOC:  $v'(Q^*) = p$ 
  - What is  $v'$ ? (Other than  $v$ 's first derivative.)

# Consumer surplus (2/3)



# Consumer surplus (3 / 3)

- ▶ Consumer surplus at a quantity  $Q^*$  and a price  $p^*$  on the demand curve is defined as the blue shaded area.
- ▶ With our consumer from before, this is:

$$\begin{aligned}\int_0^{Q^*} (p(Q) - p^*) dQ &= \int_0^{Q^*} (v'(Q) - p^*) dQ = \int_0^{Q^*} v'(Q) dQ - p^* Q^* \\ &= v(Q^*) - p^* Q^*\end{aligned}$$

- By the “Fundamental Theorem of Calculus” (FTC).
  - This says that if you integrate a derivative, you get back the original function.
- ▶ But  $v(Q^*) - p^* Q^* = U(Q^*) - Y$ .
  - Consumer surplus is a measure of utility, when agents have quasi-linear preferences.
  - With quasi-linear preferences, money is the unit of utility.
    - So CS is also a measure of the value gained by consumers.
    - Note that  $Y$  is the utility they would get when  $Q^* = 0$ .



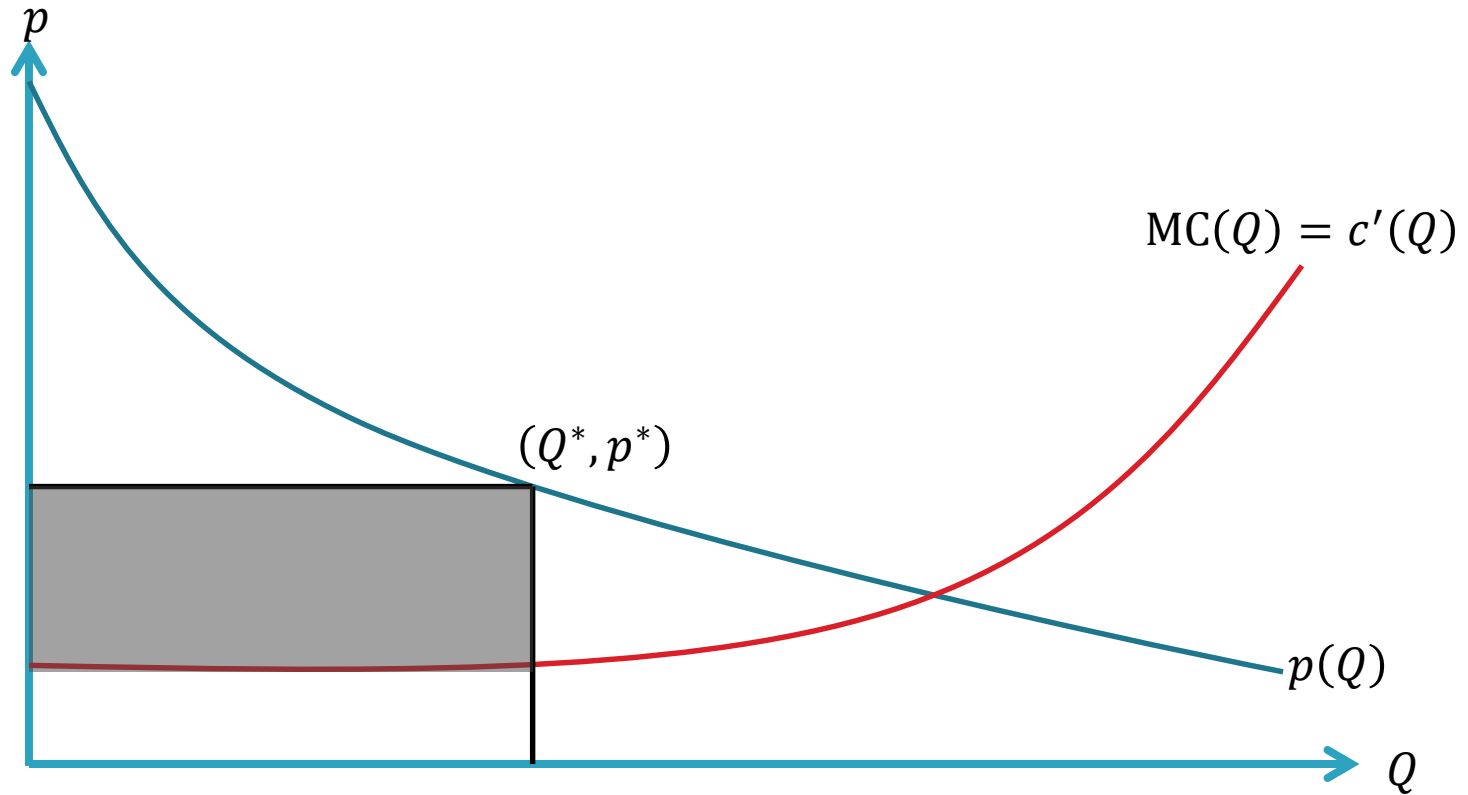
# Cost functions (OZ 3.1)

- ▶ The cost function,  $c(Q)$  gives the total cost of producing  $Q$  units.
  - $c'(Q)$  is marginal cost.
  - $\frac{c(Q)}{Q}$  is average costs.
  - When do average costs equal marginal costs?
- ▶ Suppose output is produced using  $Q = f(L)$  where  $L$  is labour, which is paid  $W$  per unit.
  - What is the cost function?
  - Example:  $Q = (L - \gamma)^\alpha$  where  $\alpha \in (0,1)$  and  $\gamma > 0$ .

# Profits (1 / 3)

- ▶ We can think of firms as either choosing prices or quantities.
- ▶ These give two different versions of the profit function:
  - $\pi(p) = pQ(p) - c(Q(p))$
  - $\pi(Q) = p(Q)Q - c(Q)$
  - If  $p(y) = Q^{-1}(y)$  for all  $y$  then these will give the same result.
- ▶ The  $p(Q)Q$  term is total revenue.
  - What is marginal revenue?

# Profits (2 / 3)



# Profits (3 / 3)

- ▶ The grey shaded area gives producer surplus at a quantity  $Q^*$  and a price  $p^*$  on the demand curve.
- ▶ This area is:

$$\begin{aligned}\int_0^{Q^*} (p^* - MC(Q)) dQ &= \int_0^{Q^*} (p^* - c'(Q)) dQ \\ &= p^* Q^* - [c(Q^*) - c(0)]\end{aligned}$$

- By the FTC again.
- ▶ But  $p^* Q^* - [c(Q^*) - c(0)] = \pi(Q^*) + c(0)$ .
  - Producer surplus measures profits.
  - Or the value gained by producers.
    - Note that  $-c(0)$  is their profit when  $Q^* = 0$ .

# Welfare

- ▶ The total value gained by all agents in the economy is consumer surplus plus producer surplus.
  - We call this welfare.
- ▶ What quantity maximises welfare?
$$W(Q) = CS(Q) + PS(Q)$$
$$= v(Q) - pQ + pQ - [c(Q) - c(0)]$$
$$= v(Q) - c(Q) + c(0)$$
- ▶ FOC:  $v'(Q^*) = c'(Q^*)$ 
  - or equivalently  $p(Q^*) = c'(Q^*)$ .
  - Perfect competition maximises welfare!

# Monopolists (1 / 2)

- ▶ A monopolist has cost function  $c(Q)$  and faces market demand curve  $p(Q)$ .
  - Profits are  $\pi(Q) = p(Q)Q - c(Q)$ .

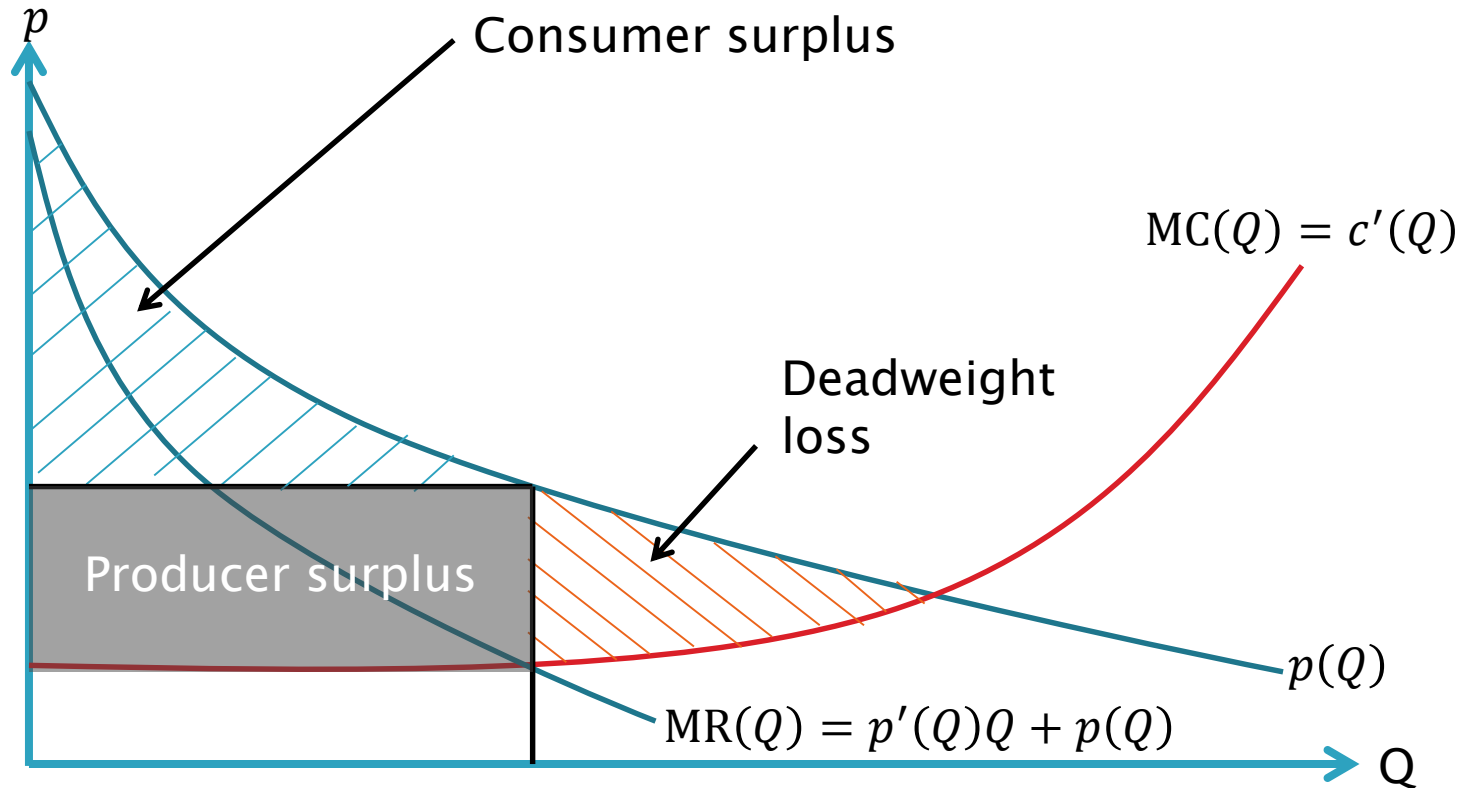
- ▶ First order condition:

$$p'(Q^*)Q^* + p(Q^*) - c'(Q^*) = 0$$

- ▶ So:

$$\begin{aligned} \text{MR}(Q^*) &= p'(Q^*)Q^* + p(Q^*) \\ &= c'(Q^*) = \text{MC}(Q^*) \end{aligned}$$

# Monopolists (2/2)



# Monopoly problems

- ▶ Suppose  $p(Q) = p_0 - p_1 Q$  and  $c(Q) = c_0 + c_1 Q$ .
  - Show that under monopoly:  $Q^* = \frac{p_0 - c_1}{2p_1}$
  - And under perfect competition:  $Q^* = \frac{p_0 - c_1}{p_1}$ 
    - So quantity is halved.
  - What are CS, PS and DWL?
  
- ▶ Suppose  $p(Q) = kQ^{-\beta}$  and  $c(Q) = c_0 + c_1 Q$ .
  - Show that under monopoly:  $p(Q^*) = \frac{1}{1-\beta} c'(Q^*)$ 
    - Mark-up pricing!



# Further problems

- ▶ Redo the problems on the previous page assuming the monopolist chooses prices rather than quantities.
  - (Using the demand curve rather than the inverse demand curve.)
  - Show your answers are equivalent.
- ▶ OZ Ex 3.4
  - Questions 3, 4, 5 and 6.
- ▶ OZ Ex 5.7
  - Questions 1, 2 and 7.
- ▶ OZ Extra exercises:
  - <http://ozshy.50webs.com/io-exercises.pdf>
  - Set #4

# Conclusions

- ▶ CS is the value gained by consumers.
- ▶ PS is the value gained by producers.
  
- ▶ Monopoly is inefficient and results in DWL.
  
- ▶ Key skills:
  - Be able to work with linear and iso-elastic demand functions.
  - Calculate elasticities etc.
  - Maximise profit, maximise welfare.